Danmarks Statistik MODELGRUPPEN

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Dokumentation af LADA

Resumé:

Papiret dokumenterer LADA modellen som den er endt med at se ud. Bemærk, at papiret er identisk med kapitel 3 i "Environmental satellite models for ADAM", hvilket forklarer den lidt specielle afsnits-, ligningsog tabelnummerering.

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Nøgleord: landbrug, disaggregering af ADAM a-erhverv, Satellitmodeller

Modelgruppepapirer er interne arbejdspapirer. De konklusioner, der drages i papirerne, er ikke endelige og kan være ændret inden opstillingen af nye modelversioner. Det henstilles derfor, at der kun citeres fra modelgruppepapirerne efter aftale med Danmarks Statistik. 1

3. The LADA-model

The LADA model describes the production in 5 agricultural subsectors constituting the agricultural sector in ADAM. These subsectors are *crops*, *cattle and milk production*, *pigs*, *poultry* and a sector defined residually, named the *q*-sector. The LADA model has two main purposes. First, the model can be used as a translation and aggregation module, which translates ESMERALDA scenarios into LADA scenarios and aggregates these scenarios into a scenario describing the agricultural sector in ADAM. Secondly, the model can be used to analyse simple and small changes in the agricultural subsectors of the model compared to some baseline scenario. For this purpose LADA has a simple description of factor demand and land use in the subsectors. In both cases the LADA-model provides a complete scenario describing the agricultural sector in ADAM as well as projections of the physical production in ESMERALDAs 16 lines of production, which are used as input in the environmental satellite model describing emissions from agriculture.

Section 3.1 describes the data construction methods and sources, which have been used during the data construction. In section 3.2 the transformation of ESMERALDA scenario into LADA scenarios is described while section 3.3 contains a description of the modelling of the subsectors production and factor demand. Section 3.4 comments on different ways of using the model.

3.1 Data construction

The five LADA subsectors: *crops*, *cattle and milk production*, *pigs*, *poultry* and the *q*-sector are a disaggregation of the ADAM agricultural sector, the *a*-sector. The objective in the data construction is to obtain subsector series for *crops*, *cattle and milk production*, *pigs* and *poultry*, which are consistent with an appropriate aggregation of the ESMERALDA lines of production. The consistency of the series is crucial when ESMERALDA scenarios are used for projection of the LADA subsectors.

The historical data concerning production and output prices in the five subsectors are published in The Agricultural Statistics and National Accounts from Statistics Denmark. Data on production and output prices describing 29 subsectors can be found in the Agricultural Statistics. These series are aggregated to the LADA subsectors crops, cattle pigs and poultry. Data from the National Accounts are mainly used to construct data describing the *q*-subsector. Table 3.1.1 below shows the connections of the LADA subsectors, the Agricultural Statistic, The National Accounts and the ESMERALDA lines of production. In Table 3.1.1 note the residual component of the agricultural sector in the Agricultural Statistics and the National Account compared to the agricultural sector in ADAM. Accordingly the *q*-subsector contains for instance fishing and forestry besides what is shown in Table 3.1.1.

Data concerning the input side of production i.e. use of energy and materials, labour and capital are constructed based on a disaggregation of the agricultural sector from the input-output tables published by Statistics Denmark into the five subsectors. The disaggregation has been performed for one year by the SJFI. Data for the remaining years have been constructed based on information of production and total input in the *a*-sector assuming that the production structure is fixed. Other sources in the data construction are historical data from SJFI and historical data from the ADAM model. Although the input side data series cannot be claimed to be historical they constitute a reasonable basis for projections of input use in the five subsectors based on ESMERALDA scenarios. A detailed description of the data and data constrution can be seen in Nielsen (2000) and Werner (2000a).

LADA subsector	Agricultural Statistics and	ESMERALDA, lines of
	National Account	production
Crops av-subsector	Total cereals, pulses ripened, seeds for sowing, seeds for manufacturing, sugar beets, potatoes	
Cattle <i>ak</i> -subsector	Milk, cattle, grass and green fodder, other crop products	dairy cattle, nurse cows, rearing cattle, calves, fodder beets, grass rotation
Pigs as-subsector	Pigs	sows, baconers
Poultry <i>ao</i> -subsector	Eggs for human consumption, poultry	Poultry
Others aq-subsector	Vegetables, mushrooms, fruit and berries, flowers, potted plants, nusery products, horses, sheep, furred animals, game, other livestock, residual	

Table 3.1.1 Construction of production and output prices

3.2 Projections based on ESMERALDA scenarios

One of the main purposes of the LADA model is to be able to translate forecasts and policy scenarios from the ESMERALDA model into scenarios of the agricultural sector in ADAM. Thereby enabling forecasts from ADAM to be based on SJFI scenarios for the agricultural sector and derivation of macroeconomic effects of agricultural and environmental policies affecting the agricultural subsectors. The ESMERALDA scenarios involve projections in both fixed and current prices. The linkage between the ESMERALDA and LADA series are modelled in a submodel of the LADA model. In the following this submodel will be referred to as *the transformation module*. The purpose of the module is to transform an ESMERALDA scenario as projection and factor demand in the five LADA subsectors using as much information from the ESMERALDA scenario as possible. The transformation module is described in detail in Werner (2000b).

The methods of projecting the variables in the LADA subsectors based on ESMERALDA scenarios differ for different categories of variables. The *aq*- subsector has to be handled separately as there is no information about this subsector in the ESMERALDA scenario.

The main categories are:

- 1) Production
- 2) Input of energy and material and gross value added
- 3) Labour force
- 4) Capital input and investment
- 5) Taxes etc.
- 6) q-subsector
- 7) Physical units

The projection of *production* series is straightforward as aggregation of ESMERALDA production series across lines of production and types of output cause no problems. The LADA subsector productions are obtained using the last historical observation in a given production series from LADA as a base and then projecting this series using the growth rate in the corresponding series from the aggregated ESMERALDA scenario. This is done in fixed and current prices and the output prices are derived.

Projecting the use of *energy and material* in the LADA subsectors based on the ESMERALDA scenario is a bit more difficult. The reason is that the ESMERALDA input structure is based on the costs of different material and energy inputs while the LADA input structure - like the input structure in ADAM - is based on an input-output model. The inputs are then aggregated to energy or material costs.

Table 3.1.2 shows the ESMERALDA cost structure and how it is linked to the LADA input structure. The first column shows the ESMERALDA costs. The second column shows the components at the input-output level in LADA, which are affected by the different ESMERALDA cost components. The third column shows the cost component, which is finally affected by the ESMERALDA costs.

In the transformation module the projection of the LADA energy and material demand is carried out at the level found in the ADAM input-output system involving supplies from 19 industries and 15 import groups. This implies that the composition of the aggregated material use changes over time in each of the agricultural subsectors in LADA. Thereby macroeconomic effects from environmental policies aimed at certain inputs in agricultural production for example fertilizers or pesticides are easier to derive. Again growth rates from an aggregation of the ESMERALDA forecast are used for projecting LADA series. Inputs at the disaggregated LADA level, which are not affected by any ESMERALDA cost component are projected using the observed value in the last historical year.

Gross Value Added is determined residually from production, energy and material use and some tax variables commented on below.

Table 5.1.2 Linking LSIVILIN		
ESMERALDA	Input from sector	LADA cost
Seeds	av, M0	Material
Fertilizer / manure	ak, as, nk, M2, M5	-
Concentrated feeds	av, nf , M0	-
Fodder roots	ak	-
Pesticides	nk, M5	-
Energy	ng, ne, M3k, M3q	Energy
Other services	qt, qq	Material
Contract operations	aq	-
Green fodder	ak	-
Labour		Labour costs
Insurance	qq	Material
Other costs	aq, qq	-
Maintenance, equipment	nm	-
Costs equipment		Capital costs, equipment
Maintenance, buildings	b	Material
Costs building		Capital costs, buildings
Maintenance, land	qq	Material

Table 3.1.2 Linking ESMERALDA costs to LADA costs

Abbreviations: av - crop subsector, ak - cattle and milk subsector, <math>as - pig subsector, aq - other agricultural, <math>ng - petroleum refineries, ne - public energy supply, nf - manufacturing of food, nm - manufacturing of macinery, nt - Shipyards etc., nk - manufacturing of chemicals, b - construction, qh - trade, qt - miscellaneous transport, qq - miscellaneous services, M0 - imports from SITC group 0, M3k - imports of coal, M3q - Imports from SITC 3 other than coal and crude oil, M5 imports from SITC 5

The ESMERALDA model projects the use of *labour* measured in hours worked as well as labour cost in each line of production. These series are used for projecting the corresponding LADA series using growth rates from the aggregated ESMERALDA scenario. From these projections further series concerning the use of labour in LADA such as hourly compensation and persons employed are derived. The partition of total employment into self-employed and wage earners is derived using ADAM assumptions on the development in hours worked per year and the share of self-employed to total employment.

The projections of series concerning *capital stocks* of buildings and machinery are the least reliable due to two particular circumstances. First, it is rather difficult to split the aggregated capital stock of equipment and buildings in the agricultural sector in ADAM into the corresponding series concerning the five LADA subsectors. Consequently the levels of capital stocks in the subsectors might not be appropriate. Secondly, the corresponding series for the use of equipment and buildings in ESMERALDA are difficult to link to the stock series in LADA. Nevertheless, these series are important as they describe the assumptions on technological development underlying the ESMERALDA scenarios.

Despite the problems, an attempt is made to derive projections of the LADA capital stock series from the ESMERALDA scenario. Again the level of capital stocks in the last historical year in the LADA data is projected using growth rates from ESMERALDA series on the total cost of using equipment and buildings respectively. Knowing the capital stocks, gross investment is determined using a relation describing

the accumulation of capital and ADAM assumptions on capital depreciation. Investment prices are derived from the ESMERALDA forecast. Based on these investment prices and assumptions on interest rates etc., the user-costs of capital are determined.

One way of avoiding the problems involved in linking the capital series could be to ignore the use of capital in the LADA model, and use the ADAM factor demand equations to determine the development of the stock of equipment and buildings in the agricultural sector contingent on the production determined in ESMERALDA. However, crucial information on the assumptions on technological development underlying the ESMERALDA scenario might be lost unless this information is extracted from the ESMERALDA scenario and introduced in the ADAM equations in some other way.

ESMERALDA provide forecasts of the subsidies received by the subsectors. The LADA model describes value added *taxes*, custom, taxes and subsidies on products and other taxes and subsidies. When projecting the subsidies the growth rate of the subsidies is used. The taxes are by and large projected using assumptions from the ADAM model.

The ESMERALDA scenario contains no information on what is happening in the q-sector, which is the residual between the agricultural sector in ADAM and agriculture as defined by SJFI. Historically, the production in the aq-sector constitutes approximately 40%. of total volume produced in the agricultural sector in ADAM. The transformation module per default projects the production in this sector to keep its relative importance unchanged compared to the last historical year. However, this procedure will not always be appropriate. For instance, this practice will exaggerate the effects of the policy when studying effects of an agricultural policy aimed at reducing pig production. The explanation being that the growth rate in the aq-production will be affected by the changed pig production. In such an analysis one solution could be to project the activity in the aq-subsector using the changes in the remaining subsectors.

Finally, series describing the production in 14 of the ESMERALDA subsectors in *physical units* are copied unaltered to the LADA scenario. These series that are used in the emission models, are measured in tons of production in the crop subsectors and number of animals in the animal subsectors.

3.3 The LADA subsectors

Besides the transformation module, the LADA model contains a description of production and factor demand in the five subsectors. This feature can be used when one wants to study environmental and macroeconomic effects following simple and small changes in the agricultural production at the subsector level compared to some baseline scenario. Below, this part of the model is described, however only main features and key equations of the model are explicitly commented. The entire model is found in Annexes 3.1 and 3.2.

It is assumed that technology in the five subsectors can be described by a Leontief production function but the determination of the production level differs among the subsectors. In the *as*-, *ao*- and *aq*-subsectors production is considered exogenous

while production in the *av*- and *ak*-subsectors are determined by the land available to the sectors.

In the *as*-, *aq*- and *ao*-subsectors it is assumed that equipment, buildings, labour, material and energy are used as inputs in production. Combined with the technology assumption the production in these subsectors can be written:

$$(3.3.1) \quad fX < k >= \min\left(\frac{fKm < k >}{bkm < k >}, \frac{fKb < k >}{bkb < k >}, \frac{Hq < k >}{bhq < k >}, \frac{fVm < k >}{bvm < k >}, \frac{fVe < k >}{bve < k >}\right)$$

where k=as, aq, ao and fX < k > is production in subsector k measured in fixed prices. fKm < k > is use of machinery, fKb < k > is use of building, Hq < k > is labour input measured in hours, fVm < k > is input of materials and fVe < k > is energy inputs. Both energy and material inputs are measured in fixed prices. bkm < k >, bkb < k >, hq < k >, bvm < k > and bve < k > are tecnological coefficients of equipment, buildings, labour, material and energy respectively.

Keeping in mind that production is considered exogenous, equation (3.3.1) and an assumption of cost minimization yield the factor demands. Note especially, that the input coefficients concerning input of material and energy are not explicit variables in the model, but are determined as sums of input-output coefficients from the disaggregated level, as:

$$(3.3.2)$$
 by $k \ge ang < k \ge ang < k \ge am3k < k \ge am3q < k > am3q$

and

(3.3.3)
$$bvm < k >= \sum_{j} a < j >< k >$$
$$j = av, ak, as, ao, aq, nf, nm, nt, nk, b, qh, qt, qq, m0, m2, m3k, m3q, m5, si$$

where the a < j > < k > are input-output coefficients at the disaggregated level of inputs. As an example the coefficient *anmas* shows how much of the input to the pig-subsector, which originates from the *nm*-industry, *manufacturing of machinery*.

Determination of production in the *av*- and *ak*-subsectors is different, since it is assumed that land is used as an input in production and that the land available to the subsectors is the limiting factor in production.

Again the technology assumption implies that production is given by: (3.3.4)

$$fX < h >= \min\left(\frac{nv < h >}{bnv < h >}, \frac{fKm < h >}{bkm < h >}, \frac{fKb < h >}{bkb < h >}, \frac{Hq < h >}{bhq < h >}, \frac{fVm < h >}{bvm < h >}, \frac{fVe < h >}{bve < h >}\right)$$

where h=av, ak and nv < h > is the land available to subsector h measured in hectares and bnv < h > is the technological coefficients associated with land in subsector h. The remaining notation is as above.

Since the amount of land available to each subsector is the limiting factor the production in subsector h is determined as

(3.3.5)
$$fX < h >= \frac{nv < h >}{bnv < h >}$$

Demands for the remaining factors are determined from equation (3.3.4), (3.3.5) and the assumption of cost minimization. Equations (3.3.2) and (3.3.3) also applies to material and energy coefficients, bvm < h > and bve < h >, in the *av*- and *ak*-subsectors.

The total amount of land available, nv, is considered exogenous. In the land allocation between the av- and ak-subsector it is assumed, that land lying fallow, nvbr, is exogenous and the use of land in the ak-subsector, nvak, is given by

(3.3.6) *nvak* = *nvsh* + *nvvg* + *nvrf*

where *nvsh*, *nvvg* and *nvrf* are land used for rotation grass, permanent grass and fodder roots respectively.

The land available to the av-subsector, nvav, is determined residually as

(3.3.7) *nvav* = *nv* – (*nvak* + *nvbr*)

This modelling of production and land used by the subsectors *av* and *ak* implies that increasing land use and thereby production in one sector leads to a decline in land use and thereby production in the other subsector given the total amount of land available and the amount of land lying fallow. This property of the LADA model is mimicing a corresponding property in the ESMERALDA model. Of course one can also change production by changing the total amount of land available or the area lying fallow. In these cases, however, one have to keep in mind that changing the area laid fallow will affect the subsidies received by the sector and a change in the total area available to agricultural production will influence the economy through various channels.

Given the land available to the av- and ak-subsectors the production volumes are determined from (3.3.5) and assuming cost minimization the demand for capital, labour, material and energy is easily derived from equation (3.3.4).

From equation (3.3.1) and (3.3.4) it is noticed that all production factors, except for land in the *av*- and *ak*-subsector are modelled as fully flexible. This is not an appropriate description of the demand for equipment and buildings, and implies that only small changes in production can be appropriately analysed directly in the LADA model. If the changes are sufficiently small it can be argued at least regarding equipment that most of the desired change in the capital stock can be gained by instantly changing investments. If one wants to analyse larger changes in production it is recommended that demand for capital are either determined by the factor demand equations in ADAM or that explicit assumptions concerning the reduction or growth of the capital stock are made.

The necessary investments consistent with the capital stocks are determined by the accumulation identity:

$$(3.3.8) \quad fI < q >< k >= fK < q >< k > -(1 - bfi < q > va) fK < q >< k >_{-1}$$

where q=m,b denotes equipment and buildings respectively and bfi < q > va are the depreciation rate for capital of type q obtained from the relevant ADAM scenario. Finally the user-cost of capital is determined for each subsector and each type of capital. The user-cost describes the cost of using one unit of capital for one period of time and is endogenous depending on investment prices.

The employment, $Q \le k >$, k = av, ak, as, ao, aq, in each subsector is derived from the labour demand measured in hours per year, $Hq \le k >$, as

(3.3.9)
$$Q < k >= \frac{Hq < k >}{Hgn} \cdot 1000$$

where *Hgn* is the agreed number of working hours per year in the manufacturing industries in ADAM. This equation yields a rather rough estimate of the number of persons employed, because the amount of hours in manufacturing and agriculture are not necessarily the same.

The taxes paid and subsidies received are modelled in 4 groups. As mentioned above the modelling of taxes is by and large identical to the modelling of these variables concerning the aggregated agricultural sector in ADAM. Subsidies on production are considered exogenous, whereas the subsidies on products are modelled as a subsidy-rate times the production in fixed prices¹.

In general, output prices as well as factor prices except user-cost of capital are exogenous in the model. Current price projections are easily derived by inflating fixed price scenarios.

To enable the calculation of emissions from the agricultural sector the production in the subsectors are disaggregated to production measured in physical units at the ESMERALDA level, that is tons of crops in the *av*-subsector and number of animals in the *ak*-, *as*-, *ao*-subsectors. It is assumed that the tons produced and number of animals per volume of production is constant implying the physical production is proportional to production in fixed prices.

¹ The taxes modelled in LADA correspond with the indirect taxes in the ADAM input-output system. These are value added taxes, Siga<j>, taxes and subsidies on specific goods, Sipa<j>, and taxes and subsidies on production, Siqa<j>.

Finally, the LADA model contains some equations used to aggregate the subsector projections to a projection describing the agricultural sector in ADAM. This part of the model is referred to as *the aggregation module*. This module has two important properties

- 1) When using the LADA model for simulation in historical years on the constructed data, the results from the aggregation module concerning the entire agricultural sector in ADAM is in fact the historical observations of this sector
- 2) When using the model for aggregation of ESMERALDA scenarios, the subsector scenarios remain unaltered through simulation

The first property implies that the aggregation module and the data are consistant with the ADAM *a*-sector. The second property implies that it is in fact the LADA subsector scenarios based on the ESMERALDA scenarios that are aggregated even though, the LADA model has to simulate to derive the scenario describing the aggregated agricultural sector in ADAM

3.4 Using the LADA model

Regardless of the use of the LADA model the output provided by the model is:

- 1) A scenario describing the activity in the agricultural sector in ADAM
- 2) Projections of the production in the ESMERALDA lines of production counted in produced tons in the crop lines and number of animals in the animal lines of production

The scenario describing the agricultural sector is used to analyse macroeconomic effects of some development in the agricultural sector. The productions in the ESMERALDA lines of production counted in physical units are used as input to the emission model calculating the emissions of N_2O , CH_4 etc. see Figure 1.1. There are three different ways of using the LADA model:

- 1) Some ESMERALDA baseline scenario is aggregated to the ADAM level and used in an ADAM forecast
- 2) Given an ESMERALDA baseline scenario and one or more alternative scenarios macroeconomic and environmental effect of policies studied in ESMERALDA can be evaluated
- 3) Given an ESMERALDA baseline scenario the macroeconomic and environmental effects of restricting production in one or more of the subsectors: crops, cattle and milk, pigs and poultry can be studied using the LADA model only

Looking at case 1) the only task of the LADA model is to aggregate the five subsectors into a scenario describing ADAMs agricultural sector and pass series on production in physical terms to the emission model. Thereafter the environmental effects of the ESMERALDA forecast are calculated in the emission model, while some macroeconomic forecast based upon the ESMERALDA forecast of the agriculture can be made in ADAM.

In case 2) the objective will typically be to evaluate environmental benefits and economic costs from introducing some policy aimed at the agricultural sector. The ESMERALDA baseline scenario is used to construct consistent scenarios describing emissions and the macroeconomy. Then alternative emission and macroeconomic scenarios can be constructed consistent with the alternative ESMERALDA scenario. The environmental benefits can be assessed by comparing the baseline emission scenario to the alternative emission scenario. While economic costs in the agriculture can be evaluated by comparing the two ESMERALDA scenarios and derived macroeconomic effects can be found by comparing the macroeconomic baseline scenario to the alternative scenarios.

Case 3) is similar to case 2) except from the fact that only simple and small change in subsector production can be analysed using the LADA model alone, and that the economic influence from the change on the agriculture must be evaluated at the LADA or ADAM level.

Annex 3.1 List of variables for LADA

The notation is standard ADAM notation, so the only news for the ADAMknowledgeable is the subsectors. A variable X appears normally in current prices, fixed prices, and as a deflator, notation is then X, fX, and pX respectively. The disaggregation of ADAM's a-sector implies that to the usual a for agriculture in ADAM will be added the following suffixes: v, k, s, f, and q for crops, cattle, pigs, poultry, and other agriculture respectively. Hence fXas is X in fixed prices for the pigs subsector.

io-coefficients have prefix *a* followed by supplying sector or import, and recipient sector, e.g. *anmas* the coefficient for supply from the *nm*-sector to subsector *s*.

Variables

a < i > < j > i = av, ak, as, af, aq, ng, ne, nf, nm, nt, nk, b, qh, qt, qq, m0, m2, m3k, m3q, m5, si, yw, yf <math>j = av, ak, as, af, aq

coefficient for supply from sector i to use in sector k

Supplies are the same as standard ADAM-supply, except for the disaggregation of sector a.

av	crops
ak	cattle
as	pigs
af	poultry
aq	others
ng	petroleum refineries
ne	energy suppliers
nf	manufacturing of food
nm	manufacturing of machinery
nt	transportation equipment
nk	chemical industry
b	construction
qh	trade
qt	other transport
qq	other services
m0	import of SITC 0: foodstuff
m2	import of SITC 2: unmanufactured goods, non food, except fuel
m3k	import of SITC 32: coal and coke
m3q	residual import of SITC 3: petroleum, electricity, and gas
m5	import of SITC 5: chemicals
si	indirect taxes, total
уw	compensation of employees
уf	gross value added

bhqa < j > j = v, k, s, f, qnecessary input of hours per unit produced in sector j

bivp < k > k = b, m

present value of expected fiscal depreciation from an investment in capital type k

bkba < j > j = v, k, s, f, qnecessary input of buildings per unit produced in sector j

bkma < j > j = v, k, s, f, qnecessary input of equipment per unit produced in sector j

bnva < j > j = v, k, s, f, qnecessary input of land per unit produced in sector j

bqsa ratio of self employed in ADAM's *a*-sector

bqsa < j > j = v, k, s, f, qratio of self employed in subsector j

btgxa degree of charging VAT on ADAM's *a*-sector

fIba < j > j = v, k, s, f, qgross fixed capital formation in buildings and civil engineering projects in subsector *j*, 1995 prices

fIma < j > j=v, k, s, f, qgross fixed capital formation in machinery, transport equipment and other equipment in subsector *j*, 1995 prices

fKba < j > j = v, k, s, f, qgross capital stock of buildings etc. in subsector j

fKma < j > j = v, k, s, f, qgross capital stock of machinery etc. in subsector *j*, 1995 prices

fKnba < j > j = v, k, s, f, qnet capital stock of buildings etc. in subsector j

fKnma < j > j = v, k, s, f, qnet capital stock of machinery etc. in subsector j

fVa < j > j = v, k, s, f, quse of energy and material in subsector *j*, 1995 prices

fVea < j > j = v, k, s, f, quse of energy in subsector *j*, 1995 prices

fVma < j > j = v, k, s, f, quse of materials in subsector *j*, 1995 prices

fXa < j > j = v, k, s, f, q

gross output in subsector *j*, 1995 prices

fYfa

gross value added in ADAM's a-sector, 1995 prices

fYfa < j > j = v, k, s, f, qgross value added in subsector *j*, 1995 prices

hgn

average working hours in manufacturing, hours per year

hqa < j > j = v, k, s, f, qvolume of hours worked in subsector j

Iba < j > j = v, k, s, f, qgross fixed capital formation in buildings and civil engineering projects in subsector *j*, current prices

Ima $\langle j \rangle$ j=v, k, s, f, qgross fixed capital formation in machinery, transport equipment, and other equipment in subsector *j*, current prices

iwbz redemption yields on bonds

iwlo banks interest rate on advances

la < j > j = v, k, s, f, qimplicit hourly compensation per wage earner in subsector j

n < j > j = km, ko, ka, kl, ss, sl, oesize of livestock in ESMERALDA subsector j

 $n \le j \ge e$ j = km, ko, ka, kl, ss, sl, oe size of livestock in ESMERALDA in subsector *j*, initial estimate for agruculture

nv total land available

nva < j > j = v, kland available to subsector j

nvbr land lying fallow

nv < j > j = sh, vg, rfhectares used in ESMERALDA subsector j

nv < j > e j = sh, vg, rf

hectares used in ESMERALDA subsector j, initial estimate for agriculture

pwa < j > j = v, k, s, f, qaverage unit costs in subsector j

pwaw average unit cost in ADAM's *a*-sector

pIba price of buildings and civil engineering projects in ADAM's *a*-sector

pIma price of machinery, transport equipment and other equipment in ADAM's *a*-sector

pVa < j > j = v, k, s, f, qdeflator for use of energy and materials in subsector j

pVea < j > j = v, k, s, f, qdeflator for use of energy in subsector j

pVma < j > j = v, k, s, f, qdeflator for use of materials in subsector j

pXa < j > j = v, k, s, f, qdeflator for gross output in subsector j

pYfa < j > j = v, k, s, f, qdeflator for gross value added in subsector j

qsa < j > j = v, k, s, f, qnumber of self employed in subsector j

qwa < j > j = v, k, s, f, qnumber of wage earners in subsector j

rpi < k > ae k = b, mexpected growth in pi < k > a

Sigxa VAT revenue from gross output in ADAM's *a*-sector

Sigxa $\leq j \geq j = v, k, s, f, q$ VAT revenue from gross output in subsector j

Sipvea revenue from duties on use of energy in ADAM's *a*-sector

Sipvea< j > j = v, k, s, f, qnet revenue from duties on use of energy in subsector j *Sipxa* net revenue from taxes on specific goods in ADAM's *a*-sector, total

Sipxa $\leq j \geq j = v, k, s, f, q$ net revenue from taxes on specific goods in subsector *j*, total

Siqa

net revenue from taxes on production in ADAM's a-sector, total

Siqa $\leq j > j = v, k, s, f, q$ net revenue from taxes on production in subsector *j*, total

Siqal

revenue from duties paid by employers on wage and salary costs in ADAM's a-sector

Siqal $\leq j > j = v, k, s, f, q$ revenue from duties paid by employers on wage and salary costs in subsector *j*

tg VAT rate

tsdsu expected marginal rate of corporation tax

t < j > j = vf, vv, vh, vb, vo, vk, vrproduction in ESMERALDA subsector *j*, tons

 $t \le j \ge e$ j = vf, vv, vh, vb, vo, vk, vrproduction in ESMERALDA subsector j, tons, initial estimate for agriculture

tvea rate of duty on *fVea*

tvea< j > j = v, k, s, f, qrate of duty on fVea < j >

ui < k > a k = b, muser-cost on capital stock of type k, in ADAM's a-sector

ui < k > a < j > k=b, m j=v, k, s, f, quser-cost on capital stock of type k, in subsector j

Va < j > j = v, k, s, f, qUse of energy and material in subsector *j*, current prices

Vea<*j*> *j*=v, *k*, *s*, *f*, *q* Use of energy in subsector *j*, current prices

Vma < j > j = v, k, s, f, qUse of materials in subsector *j*, current prices Xa < j > j = v, k, s, f, qgross output in subsector *j*, current prices

Yfa gross value added in ADAM's *a*-sector, current prices

Yfa<*j*> *j*=*v*, *k*, *s*, *f*, *q* gross value added in subsector *j*, current prices

Ywa compensation of employees in ADAM's *a*-sector

Ywa $\leq j$ > j=v, k, s, f, qcompensation of emplyees in subsector j

```
() Annex 3.2
() equations forming the LADA model
() ********
() SUB-SECTORS
() *********
() PRODUCTION
FRML _D
          fXav = (nv-(nvsh+nvvg+nvrf)-nvbr)/bnvav $
FRML D
          fXak = nvak/bnvak
                                                  $
FRML I
           Xav = pXav*fXav $
FRML I
           Xak = pXak*fXak $
          Xas = pXas*fXas $
FRML _I
          Xao = pXao*fXao $
FRML _I
           Xaq = pXaq*fXaq $
FRML _I
() ENERGY CONSUMPTION
FRML _GJR
           fVeav = (angav+aneav+am3kav+am3qav)*fXav
                                                       $
FRML _GJR
           fVeak =
                     (angak+aneak+am3kak+am3qak)*fXak
                                                       Ś
FRML _GJR
           fVeas =
                     (angas+aneas+am3kas+am3qas)*fXas
                                                       $
FRML _GJR
           fVeao =
                     (angao+aneao+am3kao+am3qao)*fXao
                                                       $
FRML _GJR
           fVeaq = (angaq+aneaq+am3kaq+am3qaq)*fXaq
                                                      $
FRML _I
           Veav = pVeav*fVeav
                                  $
FRML _I
           Veak =
                                  $
                    pVeak*fVeak
FRML _I
           Veas =
                                  $
                    pVeas*fVeas
           Veao =
FRML _I
                    pVeao*fVeao
                                  $
           Veaq = pVeaq*fVeaq
FRML _I
                                  $
() MATERIAL COBSUMPTION
FRML GJR
           fVmav = (aavav+aakav+aasav+aaoav+aagav+anfav+
                      anmav+antav+ankav+abav +aqhav+
                      aqtav+aqqav+am0av+am2av+am5av+
                      asiav)*fXav
FRML _GJR
           fVmak = (aavak+aakak+aasak+aaoak+aaqak+anfak+
                      anmak+antak+ankak+abak +aqhak+
                      aqtak+aqqak+am0ak+am2ak+am5ak+
                      asiak)*fXak
FRML _GJR
           fVmas = (aavas+aakas+aasas+aaoas+aaqas+anfas+
                      anmas+antas+ankas+abas +aqhas+
                      aqtas+aqqas+am0as+am2as+am5as+
                      asias)*fXas
FRML _GJR
           fVmao = (aavao+aakao+aasao+aaoao+aaqao+anfao+
                      anmao+antao+ankao+abao +aqhao+
                      aqtao+aqqao+am0ao+am2ao+am5ao+
                      asiao)*fXao
FRML _GJR
            fVmaq = (aavaq+aakaq+aasaq+aaoaq+aaqaq+anfaq+
                      anmaq+antaq+ankaq+abaq +aqhaq+
                      aqtaq+aqqaq+am0aq+am2aq+am5aq+
                      asiaq)*fXaq
```

\$

\$

\$

\$

\$

FRML _I	Vmav	=	pVmav*fVmav	\$
FRML _I	Vmak	=	pVmak*fVmak	\$
FRML _I	Vmas	=	pVmas*fVmas	\$
FRML _I	Vmao	=	pVmao*fVmao	\$
FRML _I	Vmaq	=	pVmaq*fVmaq	\$

() ENERGY- OG MATERIAL CONSUMPTION

FRML _I FRML _I FRML _I FRML _I FRML _I	fVav fVak fVas fVao fVaq	= = = =	
FRML _I FRML _I FRML _I FRML _I FRML _I	Vav Vak Vas Vao Vaq	= = = =	Vmav + Veav \$ Vmak + Veak \$ Vmas + Veas \$ Vmao + Veao \$ Vmaq + Veaq \$
FRML _I FRML _I FRML _I FRML _I FRML _I	pVav pVak pVas pVao pVaq	= = = =	Vak/fVak \$ Vas/fVas \$

() GROSS VALUE ADDED

FRML _	I	Yfav	=	pYfav*fYfav	\$
FRML _	I	Yfak	=	pYfak*fYfak	\$
FRML _	I	Yfas	=	pYfas*fYfas	\$
FRML _	I	Yfao	=	pYfao*fYfao	\$
FRML _	I	Yfaq	=	pYfaq*fYfaq	\$

() WAGES AND EMPLOYMENT

endnu ikke FRML _GJR FRML _GJR FRML _GJR FRML _GJR	<pre>> er det nødvendige timeinput p dannet i banken HQav = bhqav*fXav \$ HQak = bhqak*fXak \$ HQas = bhqas*fXas \$ HQao = bhqao*fXao \$ HQaq = bhqaq*fXaq \$</pre>	pr.	producerede	enhed,	er
	Qwav = HQav*(1-bqsav)*(1/hgn)*100 Qwak = HQak*(1-bqsak)*(1/hgn)*100 Qwas = HQas*(1-bqsas)*(1/hgn)*100 Qwao = HQao*(1-bqsao)*(1/hgn)*100 Qwaq = HQaq*(1-bqsaq)*(1/hgn)*100	00 00 00	\$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$		
FRML _GJR	Qsak = HQak*bqsak*(1/hgn)*1000 S Qsas = HQas*bqsas*(1/hgn)*1000 S Qsao = HQao*bqsao*(1/hgn)*1000 S	\$ \$ \$ \$ \$			

```
FRML _GJR Ywav = lav*(1-bqsav)*hqav-Siqalv
                                          $
FRML _GJR
         Ywak = lak*(1-bqsak)*hqak-Siqalk
                                          $
FRML _GJR
         Ywas = las*(1-bqsas)*hqas-Siqals
                                          $
FRML GJR
         Ywao = lao*(1-bqsao)*hqao-Siqalo
                                          $
FRML _GJR Ywaq = laq*(1-bqsaq)*hqaq-Siqalq
                                          $
() CAPITAL, COSTS OF CAPITAL AND GROSS CAPITAL FORMATION
() GROSS CAPITAL STOCKS
FRML _GJR fKmav = fXav*bkmav $
FRML
    _GJR fKmak =
                    fXak*bkmak $
FRML _GJR fKmas = fXas*bkmas $
FRML _GJR fKmao = fXao*bkmao $
FRML _GJR fKmaq = fXaq*bkmaq $
FRML _GJR fKbav = fXav*bkbav $
FRML _GJR fKbak = fXak*bkbak $
FRML _GJR fKbas = fXas*bkbas $
FRML _GJR fKbao = fXao*bkbao $
FRML _GJR fKbaq = fXaq*bkbaq $
() CAPITAL FORMATION
FRML _I fImav = fKmav-(1-bfimva)*fKmav(-1)
                                               $
FRML _I
          fImak = fKmak-(1-bfimva)*fKmak(-1)
                                               $
          fImas = fKmas-(1-bfimva)*fKmas(-1)
FRML _I
                                               $
FRML _I
          fImao = fKmao-(1-bfimva)*fKmao(-1)
                                               $
FRML _I
          fImaq = fKmaq-(1-bfimva)*fKmaq(-1)
                                               $
FRML _I
          fIbav = fKbav-(1-bfibva)*fKbav(-1)
                                               $
FRML _I
          fIbak = fKbak-(1-bfibva)*fKbak(-1)
                                               $
FRML _I
          fIbas = fKbas-(1-bfibva)*fKbas(-1)
                                               Ŝ
          fIbao = fKbao-(1-bfibva)*fKbao(-1)
FRML _I
                                               Ŝ
FRML _I
          fIbaq = fKbaq - (1 - bfibva) * fKbaq(-1)
                                               $
FRML _I
          Imav = pImav*fImav
                                $
FRML _I
          Imak = pImak*fImak $
FRML _I
          Imas = pImas*fImas $
FRML _I Imao = pImao*fImao $
          Imaq = pImaq*fImaq $
FRML _I
           Ibav = pIbav*fIbav
FRML
     _I
                                $
           Ibak = pIbak*fIbak $
FRML
     _I
           Ibas = pIbas*fIbas
FRML
     _I
                                Ś
           Ibao = pIbao*fIbao $
FRMI
     _I
           Ibaq = pIbaq*fIbaq $
FRML I
() NET CAPITAL STOCK
           fKnmav = fImav+(1-bfinmva)*fKnmav(-1) $
FRML _GJR
FRML _GJR
           fKnmak = fImak+(1-bfinmva)*fKnmak(-1) $
           fKnmas =
FRML _GJR
                    fImas+(1-bfinmva)*fKnmas(-1) $
           fKnmao = fImao+(1-bfinmva)*fKnmao(-1) $
FRML _GJR
           fKnmaq = fImaq+(1-bfinmva)*fKnmaq(-1) $
FRML _GJR
FRML _GJR
           fKnbav = fIbav+(1-bfinbva)*fKnbav(-1) $
                    fIbak+(1-bfinbva)*fKnbak(-1) $
FRML _GJR
           fKnbak =
                    fIbas+(1-bfinbva)*fKnbas(-1) $
FRML _GJR
           fKnbas =
FRML _GJR
           fKnbao =
                    fIbao+(1-bfinbva)*fKnbao(-1) $
FRML _GJR
           fKnbaq = fIbaq+(1-bfinbva)*fKnbaq(-1) $
```

FRML _I bfknmav = fKnmav/fKmav \$ FRML _I FRML _I bfknmak = fKnmak/fKmak \$ bfknmas = fKnmas/fKmas \$ FRML _I bfknmao = fKnmao/fKmao \$ FRML _I bfknmaq = fKnmaq/fKmaq \$ FRML _I bfknbav = fKnbav/fKbav \$ FRML _I bfknbak = fKnbak/fKbak \$ bfknbas = fKnbas/fKbas FRML _I \$ FRML _I bfknbao = fKnbao/fKbao \$ FRML _I bfknbaq = fKnbaq/fKbaq \$ () USER-COST () MACHINERY FRML __GJR uimav=bfknmav*pimav*(1-tsdsu*bivpm) /(1-tsdsu)*((1-tsdsu)*iwlo+bfinmva-0.5*rpimae) \$ FRML __GJR uimak=bfknmak*pimak*(1-tsdsu*bivpm) /(1-tsdsu)*((1-tsdsu)*iwlo+bfinmva-0.5*rpimae) \$ FRML __GJR uimas=bfknmas*pimas*(1-tsdsu*bivpm) /(1-tsdsu)*((1-tsdsu)*iwlo+bfinmva-0.5*rpimae) \$ FRML __GJR uimao=bfknmao*pimao*(1-tsdsu*bivpm) /(1-tsdsu)*((1-tsdsu)*iwlo+bfinmva-0.5*rpimae) \$ FRML _GJR uimaq=bfknmaq*pimaq*(1-tsdsu*bivpm) /(1-tsdsu)*((1-tsdsu)*iwlo+bfinmva-0.5*rpimae) \$ () BUILDINGS FRML _GJR uibav=bfknbav*pibav*(1-tsdsu*bivpb) /(1-tsdsu)*((1-tsdsu)*iwbz+bfinbva-0.5*rpibae) \$ FRML __GJR uibak=bfknbak*pibak*(1-tsdsu*bivpb) /(1-tsdsu)*((1-tsdsu)*iwbz+bfinbva-0.5*rpibae) \$ FRML __GJR uibas=bfknbas*pibas*(1-tsdsu*bivpb) /(1-tsdsu)*((1-tsdsu)*iwbz+bfinbva-0.5*rpibae) \$ FRML _GJR uibao=bfknbao*pibao*(1-tsdsu*bivpb) /(1-tsdsu)*((1-tsdsu)*iwbz+bfinbva-0.5*rpibae) \$ FRML _GJR uibaq=bfknbaq*pibaq*(1-tsdsu*bivpb) /(1-tsdsu)*((1-tsdsu)*iwbz+bfinbva-0.5*rpibae) \$ () COSTS OF PRODUCTION FRML _GJR pwav=(uimav*fKmav+uibav*fKbav+lav*Hqav+Veav+Vmav+siqavsiqalv)/fXav \$ FRML _GJR pwak=(uimak*fKmak+uibak*fKbak+lak*Hqak+Veak+Vmak+siqaksiqalk)/fXak \$ FRML _GJR pwas=(uimas*fKmas+uibas*fKbas+las*Hqas+Veas+Vmas+siqassigals)/fXas \$

FRML _GJR pwao=(uimao*fKmao+uibao*fKbao+lao*Hqao+Veao+Vmao+siqaosiqalo)/fXao \$ FRML _GJR pwaq=(uimaq*fKmaq+uibaq*fKbaq+laq*Hqaq+Veaq+Vmaq+siqaqsiqalq)/fXaq \$

() TAXES AND DUTIES

FRML _GJR Sigxav = tg*btgxa*(1-tg*btgxa)*Vav \$ FRML _GJR Sigxak = tg*btgxa*(1-tg*btgxa)*Vak \$ FRML __GJR Sigxas = tg*btgxa*(1-tg*btgxa)*Vas \$ FRML _GJR Sigxao = tg*btgxa*(1-tg*btgxa)*Vao \$ FRML _GJR Sigxaq = tg*btgxa*(1-tg*btgxa)*Vaq \$ FRML _GJR Sipveav = tveav*fVeav \$ FRML _GJR Sipveak = tveak*fVeak \$ FRML _GJR Sipveas = tveas*fVeas \$ FRML _GJR Sipveao = tveao*fVeao \$ FRML _GJR Sipveaq = tveaq*fVeaq \$ FRML _GJR Sipxav = tvmav*fVmav + tveav*fVeav Ś FRML _GJR Sipxak = tvmak*fVmak + tveak*fVeak \$ FRML _GJR Sipxas = tvmas*fVmas + tveas*fVeas \$ FRML _GJR Sipxao = tvmao*fVmao + tveao*fVeao \$ FRML _GJR Sipxaq = tvmaq*fVmaq + tveaq*fVeaq \$ FRML _GJ_ Sigalv = Sigal*Qwav/(Qwav+Qwak+Qwas+Qwao+Qwaq) FRML _GJ_ Siqalk = Siqal*Qwak/(Qwav+Qwak+Qwas+Qwao+Qwaq) \$ FRML _GJ_ Siqals = Siqal*Qwas/(Qwav+Qwak+Qwas+Qwao+Qwaq) \$ FRML _GJ_ Siqalo = Siqal*Qwao/(Qwav+Qwak+Qwas+Qwao+Qwaq) \$ FRML _GJ_ Siqalq = Siqal*Qwaq/(Qwav+Qwak+Qwas+Qwao+Qwaq) \$

FRML _I fXa = fXav + fXak + fXas + fXao + fXaq \$
FRML _I Xa = Xav + Xak + Xas + Xao + Xaq \$
FRML _I pXa = Xa/fXa \$

() ENERGY- og MATERIAL CONSUMPTION

FRML _I fVea = fVeav + fVeak + fVeas + fVeao + fVeaq \$
FRML _I Vea = Veav + Veak + Veas + Veao + Veaq \$
FRML _I pVea = Vea/fVea \$
FRML _I fVma = fVmav + fVmak + fVmas + fVmao + fVmaq \$
FRML _I Vma = Vmav + Vmak + Vmas + Vmao + Vmaq \$
FRML _I pVma = Vma/fVma \$
FRML _I fVa = fVav + fVak + fVas + fVao + fVaq \$
FRML _I Va = Vav + Vak + Vas + Vao + Vaq \$
FRML _I pVa = Va/fVa \$

() GROSS VALUE ADDED

FRML _I fYfa = fYfav + fYfak + fYfas + fYfao + fYfaq \$
FRML _I Yfa = Yfav + Yfak + Yfas + Yfao + Yfaq \$
FRML _I pYfa = Yfa/fYfa \$

() WAGE AND EMPLOYMENT

= HQav + HQak + HQas + HQao+ HQaq \$ FRML _I HQa FRML _I Qwa = Qwav + Qwak + Qwas + Qwao+ Qwaq \$ FRML _I Qsa = Qsav + Qsak + Qsas + Qsao+ Qsaq \$ FRML _I Ywa = Ywav + Ywak + Ywas + Ywao+ Ywaq \$ () CAPITAL, CAPITAL COSTS AND GROSS CAPITAL FORMATION FRML _I fKma = fKmav + fKmak + fKmas + fKmao + fKmaq \$ FRML _I fKba = fKbav + fKbak + fKbas + fKbao + fKbaq \$ FRML _I fKnma = fKnmav + fKnmak + fKnmas + fKnmao + fKnmaq \$ FRML _I fKnba = fKnbav + fKnbak + fKnbas + fKnbao + fKnbaq \$ FRML _I fIma = fImav + fImak + fImas + fImao + fImaq FRML _I fIba = fIbav + fIbak + fIbas + fIbao + fIbaq \$ Ima = Imav + Imak + Imas + Imao + Imaq \$ FRML _I Iba = Ibav + Ibak + Ibas + Ibao + Ibaq \$ FRML _I FRML _I pIma = Ima/fIma \$ FRML _I pIba = Iba/fIba \$ FRML _I bfknma = fKnma/fKma \$ FRML _I bfknba = fKnba/fKba \$ FRML _I uima = bfknma*pima*(1-tsdsu*bivpm)/(1-tsdsu) *((1-tsdsu)*iwlo+bfinmva-0.5*rpimae) \$ FRML _I uiba = bfknba*piba*(1-tsdsu*bivpb)/(1-tsdsu) *((1-tsdsu)*iwbz+bfinbva-0.5*rpibae) \$ FRML I la =(lav*Hqav+lak*Hqak+las*Hqas+lao*Hqao+laq*Hqaq)/hqa \$ () COSTS OF PRODUCTION FRML _GJR pwaw= (uima*fKma+uiba*fKba+la*hqa+Vea+Vma+Siqa-siqal)/fXa \$ () TAXES AND DUTIES FRML _I Sigxaa = Sigxav + Sigxak + Sigxaa + Sigxaa + Sigxaq \$ FRML _I Sipxa = Sipxav + Sipxak + Sipxas + Sipxao + Sipxaq Ś FRML _I Sipvea = Sipveav+ Sipveak+ Sipveas+ Sipveao+ Sipveaq \$ FRML _I tvma = (Sipxa-Sipvea)/fVma \$ FRML _I tvea = Sipvea/fVea \$ FRML _I Sigal = Sigalv + Sigalk + Sigals + Sigalo + Sigalq \$ FRML _I Siqa = Siqav + Siqak + Siqas + Siqao + Siqaq Ś

FRML _GJR	nkm	=	nkme*(fXak/fXake)	\$
FRML _GJR	nko	=	nkoe*(fXak/fXake)	\$
FRML _GJR	nka	=	nkae*(fXak/fXake)	\$
FRML _GJR	nkl	=	nkle*(fXak/fXake)	\$
FRML _GJR	nss	=	nsse*(fXas/fXase)/1.9	\$
FRML _GJR	nsl	=	nsle*(fXas/fXase)/1.9	\$
FRML _GJR	noe	=	<pre>noee*(fXas/fXase)*6.421</pre>	\$
FRML GJR	tvf	=	tvfe*(fXav/fXave)	\$
FRML GJR	tvv	=	tvve*(fXav/fXave)	\$
FRML GJR	tvh	=	tvhe*(fXav/fXave)	\$
FRML GJR	tvb	=	tvbe*(fXav/fXave)	\$
			tvoe*(fXav/fXave)	\$
() FRML G	JR tv	vq	<pre>= tvq*(fXav/fXave)</pre>	\$
· · · —		-	tvke*(fXav/fXave)	\$
			tvre*(fXav/fXave)	\$
—			<pre>= tvrf*(fXav/fXave)</pre>	, \$
-			<pre>= tvsh*(fXav/fXave)</pre>	\$
			= tvvq*(fXav/fXave)	\$
··· —		-	= tvoc*(fXav/fXave)	\$
-			= nvqe*fXav/fXave \$	4
··· —		-	nvshe*nvak/nvake \$	
_			nvvge*nvak/nvake \$	
			nvrfe*nvak/nvake \$	
FRML _GOR	TIVLL	- 1	IVILE IIVAK/IIVAKE Ş	